

Math 171 Calculus Handout

Derivative Rules - You do not have to memorize all of these!

GENERAL FORMULAS:

$$\begin{array}{ll}
 1. \frac{d}{dx}(c) = 0 & 5. \frac{d}{dx}(cf(x)) = c \frac{d}{dx}(f(x)) \\
 2. \frac{d}{dx}(x) = 1 & 6. \frac{d}{dx}(f(x)g(x)) = f'(x)g(x) + g'(x)f(x) \\
 3. \frac{d}{dx}(x^n) = nx^{n-1} & 7. \frac{d}{dx}\left(\frac{f(x)}{g(x)}\right) = \frac{g(x)f'(x) - f(x)g'(x)}{(g(x))^2} \\
 4. \frac{d}{dx}(f(x) \pm g(x)) = \frac{d}{dx}(f(x)) \pm \frac{d}{dx}(g(x)) & 8. \frac{d}{dx}(f(g(x))) = f'(g(x))g'(x)
 \end{array}$$

EXPONENTIAL AND LOGARITHMIC FUNCTIONS:

$$\begin{array}{ll}
 9. \frac{d}{dx}(a^x) = a^x \ln a & 11. \frac{d}{dx}(\log_a x) = \frac{1}{x \ln a} \\
 10. \frac{d}{dx}(e^x) = e^x & 12. \frac{d}{dx}(\ln x) = \frac{1}{x}
 \end{array}$$

TRIGONOMETRIC FUNCTIONS:

$$\begin{array}{lll}
 13. \frac{d}{dx}(\sin(x)) = \cos(x) & 15. \frac{d}{dx}(\tan(x)) = \sec^2(x) & 17. \frac{d}{dx}(\csc(x)) = -\csc(x)\cot(x) \\
 14. \frac{d}{dx}(\cos(x)) = -\sin(x) & 16. \frac{d}{dx}(\sec(x)) = \sec(x)\tan(x) & 18. \frac{d}{dx}(\cot(x)) = -\csc^2(x)
 \end{array}$$

INVERSE TRIGONOMETRIC FUNCTIONS:

$$\begin{array}{lll}
 19. \frac{d}{dx}(\sin^{-1} x) = \frac{1}{\sqrt{1-x^2}} & 21. \frac{d}{dx}(\tan^{-1} x) = \frac{1}{1+x^2} & 23. \frac{d}{dx}(\sec^{-1} x) = \frac{1}{x\sqrt{x^2-1}} \\
 20. \frac{d}{dx}(\cos^{-1} x) = \frac{-1}{\sqrt{1-x^2}} & 22. \frac{d}{dx}(\cot^{-1} x) = \frac{-1}{1+x^2} & 24. \frac{d}{dx}(\csc^{-1} x) = \frac{-1}{x\sqrt{x^2-1}}
 \end{array}$$

HYPERBOLIC FUNCTIONS:

$$\begin{array}{lll}
 25. \frac{d}{dx}(\sinh x) = \cosh x & 27. \frac{d}{dx}(\tanh x) = \operatorname{sech}^2 x & 29. \frac{d}{dx}(\operatorname{sech} x) = -\operatorname{sech} x \tanh x \\
 26. \frac{d}{dx}(\cosh x) = \sinh x & 28. \frac{d}{dx}(\operatorname{csch} x) = -\operatorname{csch} x \coth x & 30. \frac{d}{dx}(\coth x) = -\operatorname{csch}^2 x
 \end{array}$$

INVERSE HYPERBOLIC FUNCTIONS:

$$\begin{array}{lll}
 31. \frac{d}{dx}(\sinh^{-1} x) = \frac{1}{\sqrt{1+x^2}} & 33. \frac{d}{dx}(\tanh^{-1} x) = \frac{1}{1-x^2} & 35. \frac{d}{dx}(\operatorname{sech}^{-1} x) = -\frac{1}{x\sqrt{1-x^2}} \\
 32. \frac{d}{dx}(\cosh^{-1} x) = \frac{1}{\sqrt{x^2-1}} & 34. \frac{d}{dx}(\operatorname{csch}^{-1} x) = -\frac{1}{|x|\sqrt{x^2+1}} & 36. \frac{d}{dx}(\coth^{-1} x) = \frac{1}{1-x^2}
 \end{array}$$