

1.

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 Find C so that $f(x) = C \left(\frac{x^2 + x + 1}{(x^2 + 1)^2} \right)$ is a probability density function on $[0, \infty)$.

HINT: $\frac{x^2 + x + 1}{(x^2 + 1)^2} = \frac{x^2 + 1}{(x^2 + 1)^2} + \frac{x}{(x^2 + 1)^2}$

2.

4

 Use the Comparison Test to show the following converges.

$$\int_{12}^{\infty} \frac{x}{x^{57} + 13} dx$$